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**Actuarial  
Methods &  
Assumptions**

## 8.1-1 Actuarial Handbook for Trustees

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### **Arizona State Retirement System Actuarial Handbook for Trustees**

The enclosed handbook was written for the trustees of the Arizona State Retirement System and covers most aspects of the Actuary and his role in a pension fund's operations and planning.

Important topics covered include:

What is an Actuary?

What can Actuaries do for pension plans?

What are Actuarial Cost Methods?

What are Actuarial Assumptions?

What is an Actuarial Experience Study?

How can an Actuary help with Plan Administration?

What are Actuarial Forecasts?

How can an Actuary Help with Plan Design?

In addition, you will find a glossary of terms at the end of the Actuarial Handbook.

**The Handbook will open in a new window by clicking in this box.**

Article by Brian Murphy

The enclosed article by Brian Murphy appeared in the July 2009 issue of "Benefits and Compensation Digest" and includes important information on

- Economic Assumptions
- Payroll Growth Assumptions
- Demographic Assumptions
- Retirement Assumption
- Death After Retirement
- Unfunded Liabilities with Time Lag

The Article will open in a new window by clicking in this box.

*Actuaries go through a complicated set of assumptions to put a value on defined benefit plans. This article explains the actuarial process used for public sector pension plans, starting with a hypothetical employee's situation and then making more general assumptions. The author aims to help readers understand the many considerations that make up the process.*



**Actuarial Assumptions—  
Looking at the "Whole" Picture**  
by Brian B. Murphy

This article provides pension plan trustees a detailed look into the process public sector actuaries use to produce actuarial valuations of defined benefit (DB) plans. As an actuarial valuator in a complicated sector involving many variables, the author aims to help readers understand the many considerations that make up the process.

**Take Many for Example**

As an example plan, the author uses a year DB plan that provides a benefit of 1% above base pay for average compensation earned over 20 years of service. The plan also provides a guaranteed 2% compounded cost-of-living adjustment (COLA). Many of the calculations are based upon a sample participant—Mary, who is 40 years old, has 20 years of service and is earning \$50,000 per year on the valuation date. For the initial example, it is assumed that Mary will retire at the age of 60 and live to be 85 years old. Mary will receive pay increases of 3% per year with her price to retirement and will receive the plan's annual 2% compounded COLA each year following retirement. Pay increases and COLA will occur on the birthday on which every other DB event that happens to Mary. Later in the article, the assumptions will be made more general.

In presenting a valuation of a DB pension plan, one of the first steps an actuary must develop is the present value of future benefits. The present value of an amount of money payable to the beneficiary in the amount of money that it would build today, would accumulate to the amount that is payable (contingent).

- Investment return.
- Probability that annuity will be paid.

The first step, of course, is to project Mary's pension liability. The author will simplify the calculations by assuming that Mary will retire at the age of 60—in other words, the most likely, because discussed in the future here. The calculation is shown in Exhibit 1.

Mary's annual pension (payable monthly at the age of 60) will be \$22,000—exactly 44% of her three-year average salary. Because 1% times 20 years is 20%, and annual 3% pay raises pay the year after, it is assumed that her average monthly pension will be 44% of her average monthly salary. Also, the retirement date, partly due to the effects of inflation. Hence, the average rate of increase to the account position of pension age. For the balance of the article, we will assume an inflation rate of 3% per year, and part of that due to the increase in Mary's total average pay.

In calculating the present value of Mary's pension, the author uses an interest assumption of 8% per year. Broadly, either the present value, considerations regarding the amount of the payment to be made each year, the probability that the payment will be made and the interest discount. These assumptions are that Mary will live to exactly age 85, the probability of payment is 100% (certain) and 8% thereafter. The results are shown in Exhibit 1. In the table, the present value is initially discounted back to Mary's retirement age (60), and is then further discounted back to her age on the valuation date (age 40).

Now that the basic present value calculation has been shown, the author discusses more general assumptions that can be used in that calculation. The author also discusses Exhibit 1 and the pay growth assumption. Exhibit 1 defines the pay assumptions necessary to produce the valuation.

**Economic Assumptions**

The key economic assumptions in the investment return assumption (called the interest rate) assumption, the discount rate, and the payroll growth rate. 3% inflation based on the same underlying price inflation assumption.

The interest rate assumption typically ranges from 3% to 8% based on the price inflation and a small risk-free rate on the risk-free rate. The range of 3% to 8% represents an assumed return to taking equity risk.

The pay increase assumption typically consists of three parts:

1. A component such as 1% assumed to be due to pay price inflation.
2. A component such as 1% assumed to be due to productivity growth and demographic assumptions.
3. A component varying by age on services that reflect the individual's performance.

When Mary's pension was projected, it was assumed that Mary would always get a 4% pay increase per year. In the future, that might have been a 3% inflation assumption, a 1% general productivity assumption and a 0% individual performance assumption. Each assumption would be called a "rate" value. Table IV shows a general pay increase assumption to project the final average earnings of a person who is hired at \$50,000 per year and works to the end of a 35-year career.

**The Payroll Growth Assumption**

When collective liabilities are being accounted for as a level percentage of payroll, the assumption must be made regarding the rate of payroll growth. If a constant proportion is assumed (always the case), the payroll growth assumption will result in the level percentage of payroll. In those examples, the payroll growth assumption would be 3% (3% plus 0%). In other words, general inflation and the budgetary growth with price inflation. Hence, actuaries must be careful to address an inflation as a level percentage of pay and the payroll growth assumption higher than inflation, understanding one should. Actuaries with a long-term trend, and the payroll growth rate 3% inflation based on the same underlying price inflation assumption.

Continued on next page

**ADDITIONAL Resources**

**More Information**

For related article information, see [www.dfp.org/publications/assumptions](#)

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**Book**

**Handbook of Employee Benefits and Administration**

Christophers C. Beckwith and David D. Coughlin, authors. Eighth and Eleventh Editions. 2008. Item #DFW 512011-11. Members \$129.95. For more book details, see [www.dfp.org/books/price/512011-11](#). To order, call 800.333.3337, ext. 4.

20 July 2009 • www.dfp.org • Benefits & Compensation Digest

July 2009 • www.dfp.org • Benefits & Compensation Digest

Page 241 of 294

### 8.3-1 Actuarial Methods and Assumptions

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In establishing a retirement plan, a public employer is promising to pay benefits that will come due in the future. Generally these benefits can be paid in one of two ways: either "pay-as-you-go", or through some form of reserve funding.

Under the "pay-as-you-go" method, the monies required to pay retirement benefits are obtained when the benefits come due to current retirees. This approach invariably results in contribution rates, which increase, as a percent of active member payroll, over time.

Under a reserve funding method, contributions are made toward the present value of the benefits being earned by active employees. Those contributions, together with investment income, are intended to accumulate sufficient assets to cover the benefit obligations by the time employees retire. Under a reserve funding approach, contribution rates are often expected to be a level or declining percent of payroll over time.

### **Actuarial Valuation Methods**

When funds for employee benefits are accumulated on a reserve-funding basis, actuarial valuations are used to compute the contributions required to fund the long-term value of the benefits. Using assumptions about employee demographics, rates of investment return, and increases in employee compensation, the actuary calculates the contributions necessary for the orderly accumulation of assets needed to pay benefits when due.

### 8.3-3 Actuarial Methods and Assumptions

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#### **Actuarial Valuation Methods**

Actuaries use different actuarial methods to calculate the contributions required to fund the plan. A prior survey conducted by the GFOA indicated that four funding methods were commonly used by public retirement plans:

**Entry Age**

**Aggregate**

**Frozen Entry Age**

**Projected Unit Credit**

Although all of the above methods will result in sufficient assets becoming available to meet benefit payments over the long run, the different methods are likely to result in different patterns of contributions over the intermediate period.

### **Actuarial Valuation Methods**

These may be important to an employer, since some patterns offer greater consistency in contributions from year to year.

The majority of the PPCC respondents used the entry age actuarial method. 66 percent of the respondent systems used the entry age method, nine percent used the projected unit credit method, seven percent used the aggregate method, seven percent used the frozen entry age method, and the remainder used various other actuarial methods.

In general, respondents administered by state governments were somewhat more likely to use the entry age method than respondents administered by local governments. Eighty-two percent of the systems administered by state governments used the entry age method, compared with 53 percent of the local systems. It is also interesting to note that 11 percent of the respondents administered by local governments used the projected unit credit method.

### **Actuarial Valuation Frequency**

The frequency with which the actuarial valuations are conducted is important to the proper funding of a retirement plan. Since valuations are based on assumptions which may change over time, the calculated contributions may not be accurate if the assumptions are not periodically updated. The majority of respondents indicated that they conducted actuarial valuations annually.

78 percent conducted actuarial valuations every year; 13 percent every two years; 3 percent every three years; and 2 percent every four or more years. All told, 91 percent of the respondents conducted actuarial valuations at least every two years. Smaller systems, systems in the Northeast and West, and systems administered by local governments were somewhat less likely to conduct annual valuations than their counterparts. On the other hand, systems serving teachers and other school employees were somewhat more likely to perform annual valuations. However, these differences essentially disappear when the frequency of the valuation is extended to two years.



### **Actuarial Assumptions Regarding Investment Return**

The assumptions used by actuaries to calculate the funding requirements of the PERS play an important role in determining the amount of the computed contributions. Because it is impossible to know the future, a variety of assumptions must be made concerning rates of investment return, pay increases, withdrawal from employment, and mortality. Of these, the assumptions regarding investment return and salary increase are especially critical, since even small changes in these assumptions can result in large changes to computed contributions.

The mean actuarial assumption regarding the investment rate of return for all systems was 7.76 percent. As asset size increases, so does the assumed rate of return. On average, systems with assets of less than \$100 million assumed annual returns of 7.64 percent while systems with \$10 billion or more assumed returns of 7.91 percent. It is interesting to note that, while these differences are statistically significant, they are also very narrow, amounting to only 27 basis points on average between the larger and smaller systems.

### **Actuarial Assumptions Regarding Salary Increase**

In addition to assumptions about the long-term rates of return on investments, systems must also establish assumptions about the long-term rate of growth in employees' salaries. These assumptions usually include estimates of increases due to merit and seniority as well as inflation, although the survey respondents often did not show these components separately.

Assumed salary increases (including both merit and inflationary increases) ranged over a wide scale, with two-thirds of the respondents reporting values between 5.0 and 7.0 percent. Exhibit IV-4 shows the distribution of assumptions regarding salary increases, which averaged 5.93 percent for all systems. As with investment return, the values for the smaller systems were lower than for the larger systems. On average, respondent systems with less than 1,000 members assumed rates of salary increase of 5.89 percent, while systems with 100,000 members or more assumed salary increases of 6.46 percent.

It should be noted that these figures include both inflation and merit/step increases. Although not all systems disaggregated their salary assumptions into these various Subcomponents, the analysis of the systems that did indicates that the assumptions about inflation averaged 5.01 percent.

### **Conclusions**

The majority of respondents accumulated the monies necessary to pay retirement benefits through a reserve funding method which, in most cases, was based on the entry age cost method. Actuarial valuations were carried out frequently, usually on an annual basis, and over 90 percent of the respondents performed actuarial valuations at least every two years.

The average assumed investment rate of return was 7.76 percent, and the average assumed rate of total salary increase was 5.93 percent. The average assumed rate of inflation was 5.01 percent for the respondents who reported this assumption separately.

#### 8.4-1 GFOA Recommended Practices

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The enclosed information is an excerpt from the GFOA (Government Finance Officers Association) web site and describes the GFOA recommended best practices for diligent and responsible management of a pension fund plan.

**[Click here to open the article in a new window](#)**